

8-2 Multiplying and Dividing Radical Expressions

Product Property of Radicals

If $\sqrt[n]{a}$ and $\sqrt[n]{b}$ are real numbers, and $n \geq 2$ is an integer, then

$$\sqrt[n]{a} \cdot \sqrt[n]{b} = \sqrt[n]{ab}$$

Simplify

$$\sqrt{5} \cdot \sqrt{3}$$

$$\sqrt{5 \cdot 3} = \sqrt{15}$$

$$\sqrt[3]{2} \cdot \sqrt[3]{13}$$

$$\sqrt[3]{26}$$

$$\sqrt{11} \cdot \sqrt{7}$$

$$\sqrt{77}$$

$$\sqrt[4]{6} \cdot \sqrt[4]{7}$$

$$\sqrt[4]{42}$$

Handwritten diagram showing prime factorization of 42: 42 is written as 6 * 7, and 6 is written as 3 * 2. Arrows point from 6 to 3 and 2, and from 7 to 7.

Multiply

$$\sqrt[5]{6c^1} \cdot \sqrt[5]{7c^2}$$

$$\sqrt[5]{42c^3}$$

$$c^1 \cdot c^2 = c^3$$

$$\sqrt[7]{5p} \cdot \sqrt[7]{4p^3}$$

$$\sqrt[7]{20p^4}$$

Multiply and Simplify. Assume all variables are greater than zero.

$$3\sqrt[3]{4x} \cdot \sqrt[3]{2x^4}$$

$$3\sqrt[3]{8x^5}$$

$$= 6x\sqrt[3]{x^2}$$

$$\sqrt[4]{27a^2b^5} \cdot \sqrt[4]{6a^3b^6}$$

$$\sqrt[4]{162a^5b^{11}}$$

$$3ab^2\sqrt[4]{2ab^3}$$

Multiply and Simplify. Don't forget to look for absolute value!

$$\sqrt{6} \cdot \sqrt{8}$$

$$4\sqrt{3}$$

$$4\sqrt[3]{8a^2b^5} \cdot \sqrt[3]{6a^2b^4}$$

$$8ab^3\sqrt[3]{6a}$$

Quotient Property of Radicals

If $\sqrt[n]{a}$ and $\sqrt[n]{b}$ are real numbers, $b \neq 0$, $n \geq 2$ is an integer, then

$$\frac{\sqrt[n]{a}}{\sqrt[n]{b}} = \sqrt[n]{\frac{a}{b}}$$

Simplify the following radicals

$$\sqrt{\frac{18}{25}}$$

$$\frac{\sqrt{18}}{\sqrt{25}} = \frac{3\sqrt{2}}{5}$$

Handwritten notes: Prime factorization of 18 is $2 \times 3 \times 3$ (circled 3s) and of 25 is 5×5 (circled 5s).

$$\sqrt[3]{\frac{6z^3}{125}}$$

$$\frac{\sqrt[3]{6z^3}}{\sqrt[3]{125}} = \frac{z^3\sqrt{6}}{5}$$

Handwritten notes: Prime factorization of 125 is $5 \times 5 \times 5$ (circled 5s). A red arrow points from the original expression to the simplified one.

$$\sqrt[4]{\frac{10a^2}{81b^4}}$$

$$\frac{\sqrt[4]{10a^2}}{3b}$$

Handwritten notes: Prime factorization of 81 is $3 \times 3 \times 3 \times 3$ (circled 3s). A blue arrow points from the original expression to the simplified one.

Simplify the following radicals

$$\sqrt{\frac{13}{49}}$$

$$\frac{\sqrt{13}}{\sqrt{49}} = \frac{\sqrt{13}}{7}$$

$$\sqrt[3]{\frac{27p^3}{8}}$$

$$\frac{\sqrt[3]{27p^3}}{\sqrt[3]{8}}$$

$$\frac{3p}{2}$$

$$\sqrt[4]{\frac{3q^4}{16}}$$

$$\frac{\sqrt[4]{3q^4}}{\sqrt[4]{16}}$$

$$\frac{q\sqrt[4]{3}}{2}$$

Simplify assuming all variables are greater than or equal to zero.

$$\frac{\sqrt{24a^3}}{\sqrt{6a}}$$

$$\sqrt{\frac{24a^3}{6a}}$$

$$\sqrt{4a^2} = 2a$$

$$\frac{-2\sqrt[3]{54a}}{\sqrt[3]{2a^4}}$$

$$-2\sqrt[3]{\frac{54a}{2a^4}}$$

$$-2\sqrt[3]{27a^{-3}}$$

$$= -6a^{-1} = -\frac{6}{a}$$

Simplify and assume all variables are greater than zero.

$$\frac{\sqrt{12a^5}}{\sqrt{3a}}$$

$$\sqrt{4a^4}$$

$$2a^2$$

$$\frac{\sqrt[3]{-24x^2}}{\sqrt[3]{3x}}$$

$$\sqrt[3]{-8x} = -2\sqrt[3]{x}$$



Rationalizing Radical Expressions

No Radicals in denominator
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$$\frac{1 \cdot \sqrt{7}}{\sqrt{7} \cdot \sqrt{7}} = \frac{\sqrt{7}}{\sqrt{49}} = \frac{\sqrt{7}}{7}$$

$$\frac{\sqrt{5} \cdot \sqrt{12}}{\sqrt{12} \cdot \sqrt{12}} = \frac{\sqrt{60}}{12} = \frac{2\sqrt{15}}{12} = \frac{\sqrt{15}}{6}$$

$\sqrt{60} \begin{cases} 12 \\ 5 \\ 3 \end{cases}$

$$\frac{2 \cdot \sqrt{2x}}{3\sqrt{2x} \cdot \sqrt{2x}} = \frac{2\sqrt{2x}}{3 \cdot 2x} = \frac{2\sqrt{2x}}{6x} = \frac{\sqrt{2x}}{3x}$$

Rationalize the following

$$\frac{1}{\sqrt{3}}$$

$$\frac{\sqrt{5}}{\sqrt{8}}$$

$$\frac{5}{\sqrt{10x}}$$