

2-3 Elimination

Objectives:

I can solve a system by elimination and determine the number of solutions

I can verify a solution

Vocabulary

Elimination: get rid of something

^{one} Solution: ordered pair (x, y)

* infinitely many solutions: thing eliminate, get true statement

* No solution: things eliminate, $4 = 4$
get false statement
 $0 = 7$

Elimination

DID NOT
7x eliminate!

$$\begin{array}{r} 4x \\ -4x \\ \hline 0 \end{array}$$

$$\begin{array}{r} -10 \\ 10 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 7x \\ \hline 14x \end{array}$$

$$\begin{array}{r} -x \\ x \\ \hline 0 \end{array}$$

$$\begin{array}{r} 2x - y = 1 \\ + \\ -2x + 2y = 3 \\ \hline \end{array}$$

Final
ANSWER

$$y = 4$$

$$(2.5, 4)$$

$$\Delta \quad \begin{array}{r} 2x - 4 = \\ + 4 \end{array} =$$

$$\begin{array}{r} 2x = 5 \\ \hline 2 \quad 2 \end{array}$$

$$x = 2.5$$

Solve the following systems by elimination
(verify)

$$\begin{array}{r} -4x + 3y = -3 \\ + 4x - 5y = 5 \\ \hline \end{array}$$

$$\frac{-2y}{-2} = \frac{2}{-2}$$

$$y = -1$$

$$-4x + 3(-1) = -3$$

$$\begin{array}{r} -4x - 3 = -3 \\ \quad +3 \quad +3 \\ \hline \end{array}$$

$$\begin{array}{r} -4x = 0 \\ \hline -4 \quad -4 \end{array}$$

$$(0, -1)$$

$$x = 0$$

$$\begin{array}{r} y - 2x = 1 \\ - (y + x = 4) \\ \hline y - x = -4 \\ \hline -3x = -3 \\ \hline x = 1 \end{array}$$

$$y - 2(1) = 1$$

$$\begin{array}{r} y - 2 = 1 \\ +2 \quad +2 \\ \hline y = 3 \end{array}$$

$$(1, 3)$$

Solve the following systems by elimination

$$5x + 6y = -8$$

$$(2x + 3y = -5) \cdot 2$$

$$\frac{-4x - 6y = 10}{}$$

$$x = 2$$

$$5(2) + 6y = -8$$

$$10 + 6y = -8$$

$$\frac{-10}{}$$

$$6y = -18$$

$$\frac{6}{6} \cdot \frac{-18}{6}$$

$$(2, -3)$$

$$(-3, -5)$$

$$\begin{array}{r} \cancel{8x - 4y = 8} \\ -8x + y = 19 \end{array} +$$

$$8x - 8y = 16$$

$$\frac{-7y = 35}{\frac{-7}{-7} \cdot \frac{35}{-7}}$$

$$y = -5$$

$$y = -5$$

$$-0x + (-5) = 19$$

$$-0x = 24 \quad +5 \quad +5$$

$$x = -3$$

$$8x - 8(-5) = 16$$

$$8x + 40 = 16$$

$$\frac{-40}{} \quad \frac{-40}{}$$

$$8x = -24$$

$$x = -3$$

Solve the following systems by elimination

$$\cancel{5x} - 4y = -11$$

$$\cancel{-5x} + 5y = 15$$

$$\cancel{*3x} + 2y = 11$$

$$\cancel{= 3(x + 5y = 8)} +$$

$$\cancel{-3x - 15y = -21}$$

$$(3, 1)$$

$$-13y = -13$$

$$y = 1$$

$$3x + 2(1) = 11$$

$$3x + 2 = 11$$

$$\begin{array}{r} -2 \quad -2 \\ 3x + 2 = 11 \\ -2 \quad -2 \\ \hline 3x = 9 \end{array}$$

$$3x = 9$$

$$x = 3$$

Example: A buffet has one price for adults and another price for children. The Taylor family has 2 adults and 3 children and their bill was \$40.50. The Wong family has 3 adults and 1 child and their bill was \$38. What is the price for adults and children at the buffet?

$a = \text{adult } \$$

$c = \text{child } \$$

Taylor: $2a + 3c = \$40.50$

Wong: $(3a + 1c = 38) \times 3$
 $-9a - 3c = -114 \quad +$

$$2(10.5) + 3c = 40.5 \quad \frac{7a}{-7} = \frac{-73.5}{-7}$$

$$21 + 3c = 40.5$$

$$-21 \quad -21 \quad a = 10.5$$

$$\frac{3c}{3} = \frac{19.5}{3} \quad c = 6.50$$

adult meal costs \$10.50

child meal costs \$6.50